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# Rotordynamic Fluid Film Bearing Analysis:

## Navier-Stokes Equations vs. Reynolds Equation

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# *Presentation Overview*

## ➤ Objective

- Illustrate Difference Between Governing Equation Options
  - » Navier-Stokes (N-S)
  - » Reynolds Equation (ReEq)

## ➤ Methodology

- Presentation will Focus on Select Bearing Analysis Results
  - » Prediction of Journal Location within its Bore
    - Dynamic Coefficients are Directly Related to Journal Location
  - » Various Flow Conditions
    - Highly Laminar to Fully Turbulent
- Presentation is Not Going to Cover the Math
  - » Math is Well Documented in Many Sources, including:
    - Fluid Film Lubrication Theory & Design by Andres Z. Szeri, 1998

# *Table of Contents*

## ➤ Background

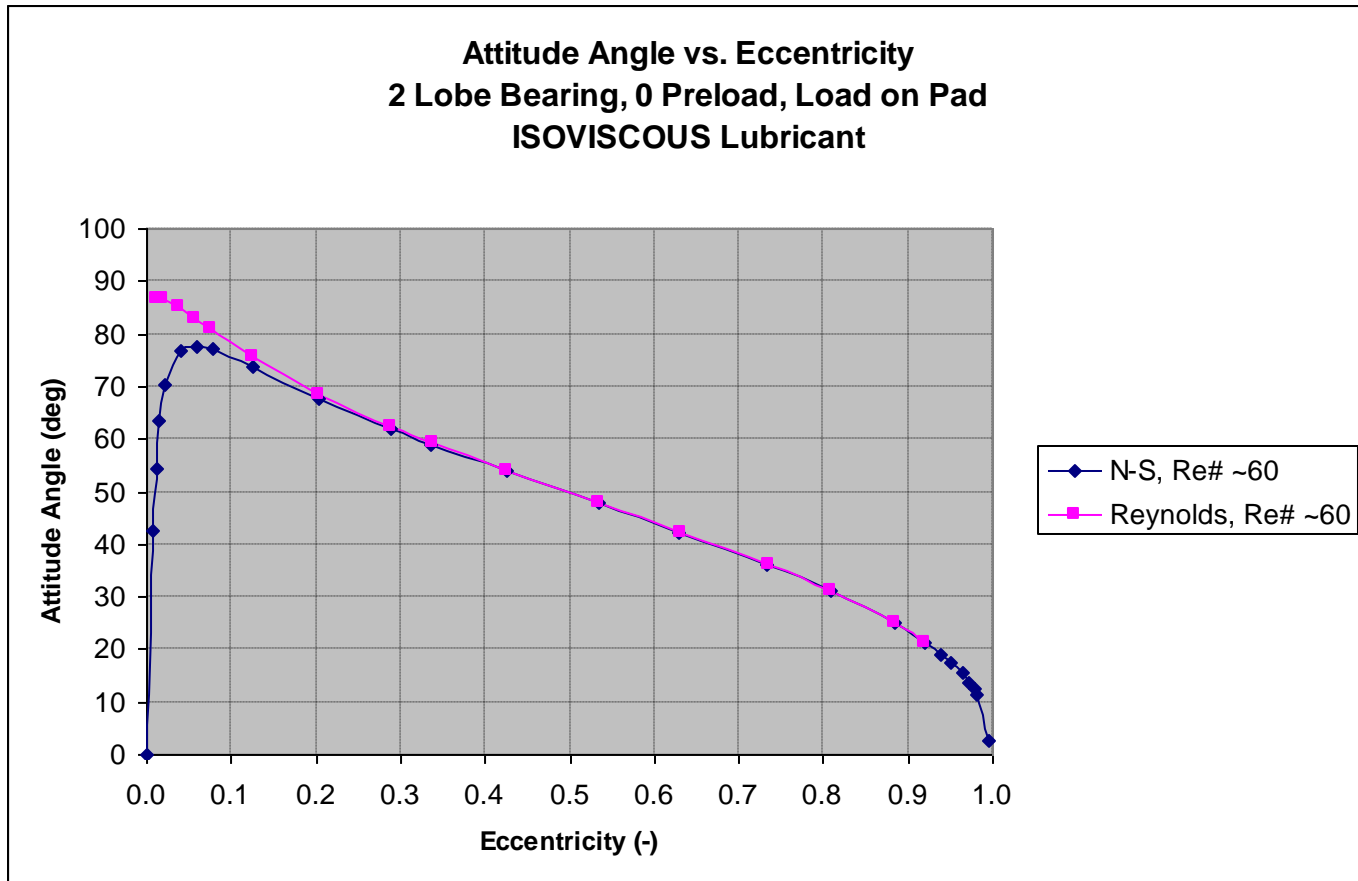
- Reynolds Equation is Derived From the N-S Equations by Making Simplifying Assumptions
  - » Primary Assumption: Neglect Inertia Effects
- Implications of Ignoring Inertia
  - » Eliminates Momentum Equations
    - Primary Advantage:
      - Greatly Simplifies Solution  
Faster Runs, Simpler Solution Algorithm
    - Primary Disadvantage:
      - Loss of Ability to Accurately Model Basic Bearing Effects
        - Shear Stress
        - Turbulence
        - Rotor Speed
        - Surface Roughness
        - Fluid Compressibility
        - Non-Newtonian Fluids
        - Low Eccentricity Bearings

# *Sample Calculations: Set 1*

## ➤ Journal Bearing Analysis

- 2 Lobe Fixed Geometry Bearing
  - » Circular Bore (Zero Preload)
  - » Load on Pad
  - » Isoviscous Lubricant
  - » Rotor Diameter = 2 inches
  - » Rotor Speed = 10000 rpm
- **Maximum Reynolds Number (Re#) on Loaded Bearing Surface: ~60**

# Highly Laminar Flow Results



# *Highly Laminar Flow Results*

## ➤ Journal Bearing Analysis: Max. Re# ~60

- Discussion of Results:

- » **Note: All Data Points Shown are For Identical Applied Loads**
- » Reynolds Equation Results Are Virtually Identical N-S Results For Operating Conditions that Yield High Journal Eccentricities ( $e > 50\%$ ) & Highly Laminar Flow
- » Inertia Affects the Solution For Operating Conditions that Yield Low Journal Eccentricities ( $e < 50\%$ ) & Highly Laminar Flow
  - $e < 20\%$ : Inertia Effects are Significant
  - $e < 10\%$ : Inertia Effects Dominate the Solution

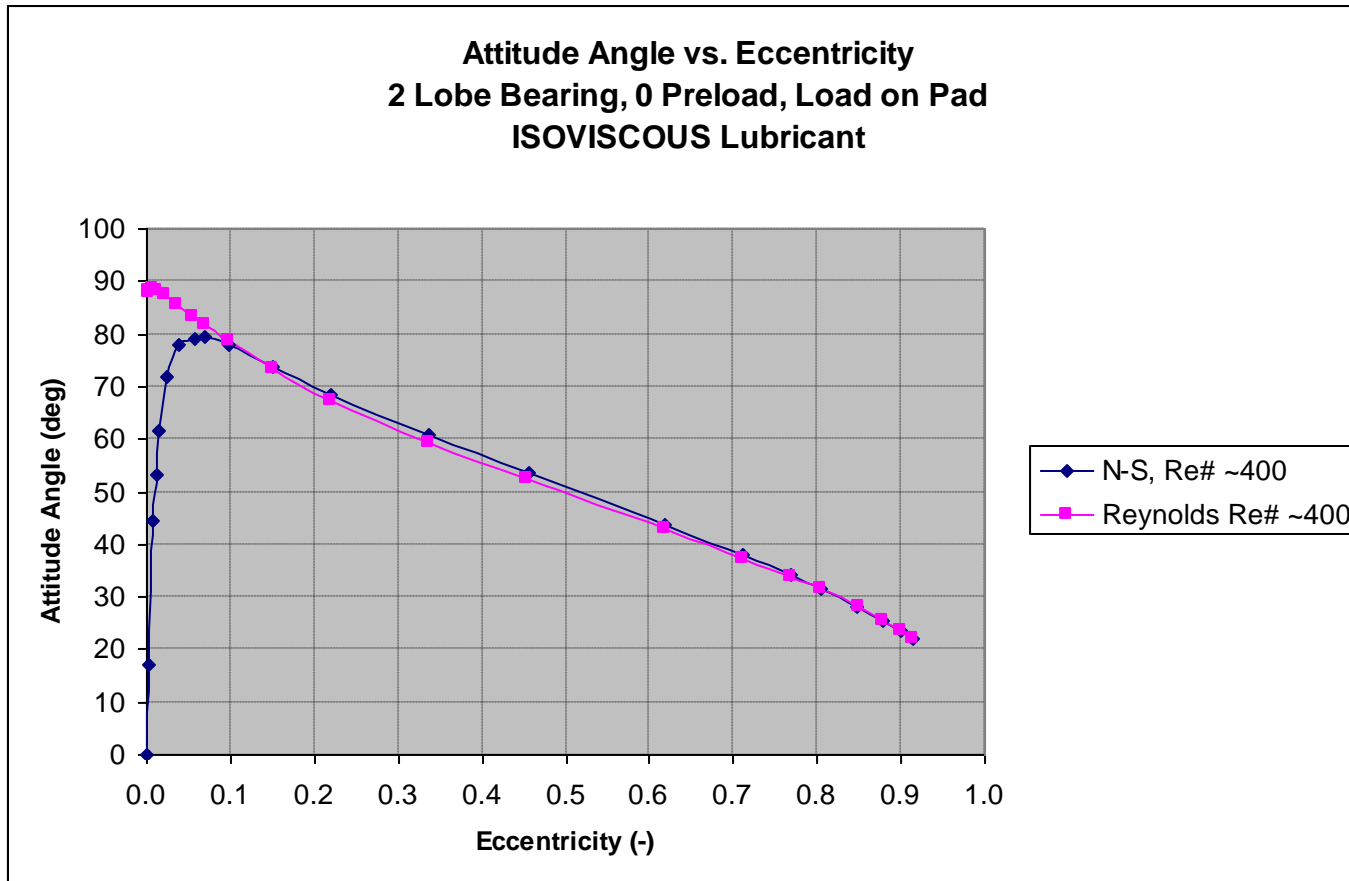
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# *Sample Calculations: Set 2*

## ➤ Journal Bearing Analysis

- 2 Lobe Fixed Geometry Bearing
  - » All Conditions Identical to Set 1 Calculations Except Rotor Speed
  - » Rotor Speed = 60000 rpm
- **Maximum Re# on Loaded Bearing Surface: ~400**

# Laminar Flow Results





# *Laminar Flow Results*

- **Journal Bearing Analysis: Max. Re# ~400**
  - **Discussion of Results:**
    - » **Note: All Data Points Shown are For Identical Applied Loads**
    - » **Reynolds Equation Results Are Nearly Identical to N-S Results For Operating Conditions that Yield High Journal Eccentricities ( $e > 75\%$ ) & Laminar Flow**
    - » **Inertia Affects the Solution For Operating Conditions that Yield Low Journal Eccentricities ( $e < 75\%$ ) & Laminar Flow**
      - $e < 60\%$ : Inertia Effects are Significant
      - $e < 10\%$ : Inertia Effects Dominate the Solution

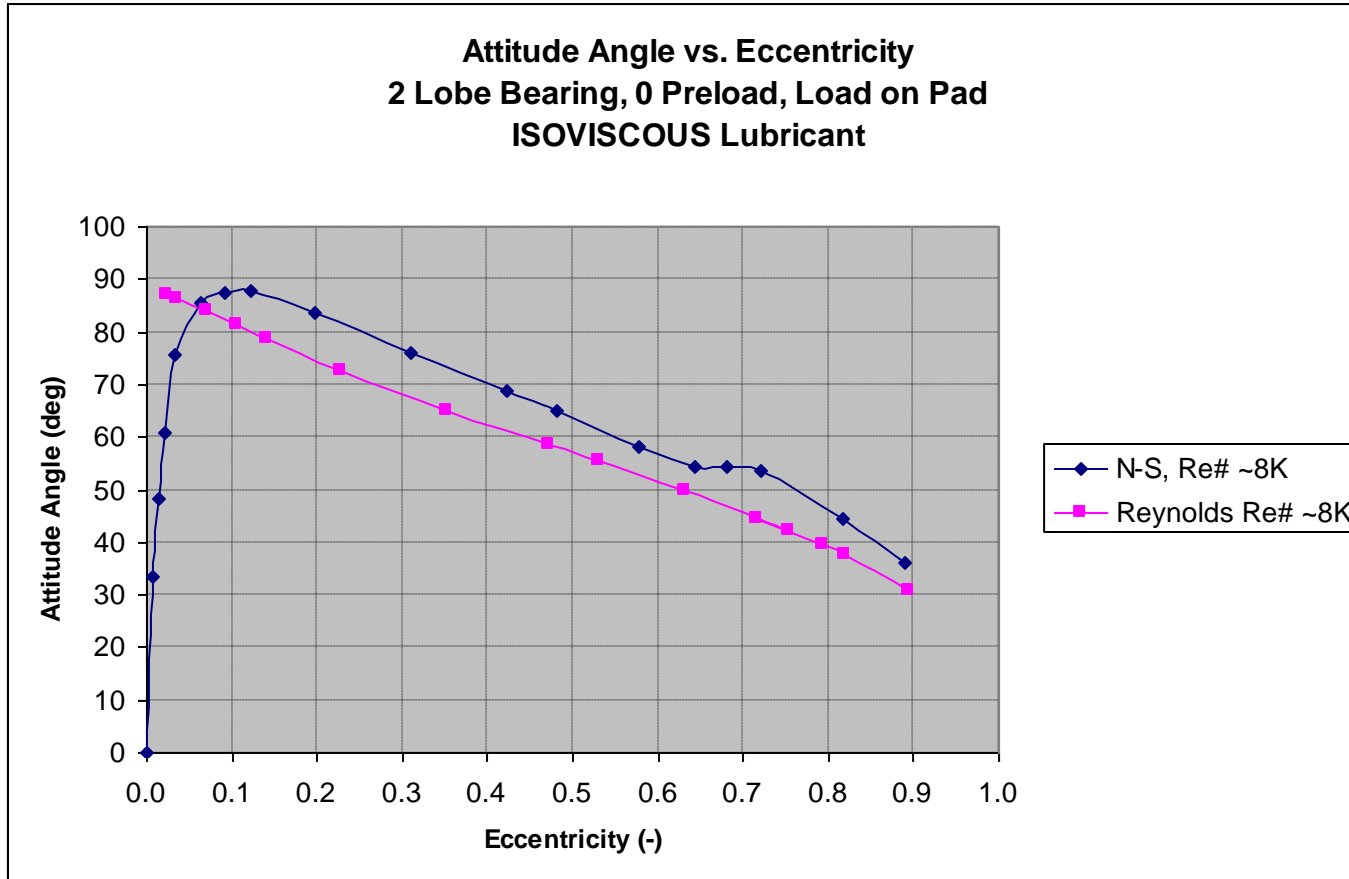
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# *Sample Calculations: Set 3*

## ➤ Journal Bearing Analysis

- 2 Lobe Fixed Geometry Bearing
  - » All Conditions Identical to Set 1 Calculations Except Rotor Speed and Viscosity
  - » Rotor Speed = 40000 rpm
- **Maximum Re# on Loaded Bearing Surface: ~8000**

# Transitional Flow Results



# *Transitional Flow Results*

- **Journal Bearing Analysis: Max. Re# ~8000**
  - **Discussion of Results:**
    - » **Note: All Data Points Shown are For Identical Applied Loads**
    - » **Reynolds Equation Inaccurate At All Eccentricities**
      - **Results Only In the Ball Park for The Two Highest Eccentricity Cases ( $e > 80\%$ )**
    - » **Inertia Effects Substantial At All Eccentricities**

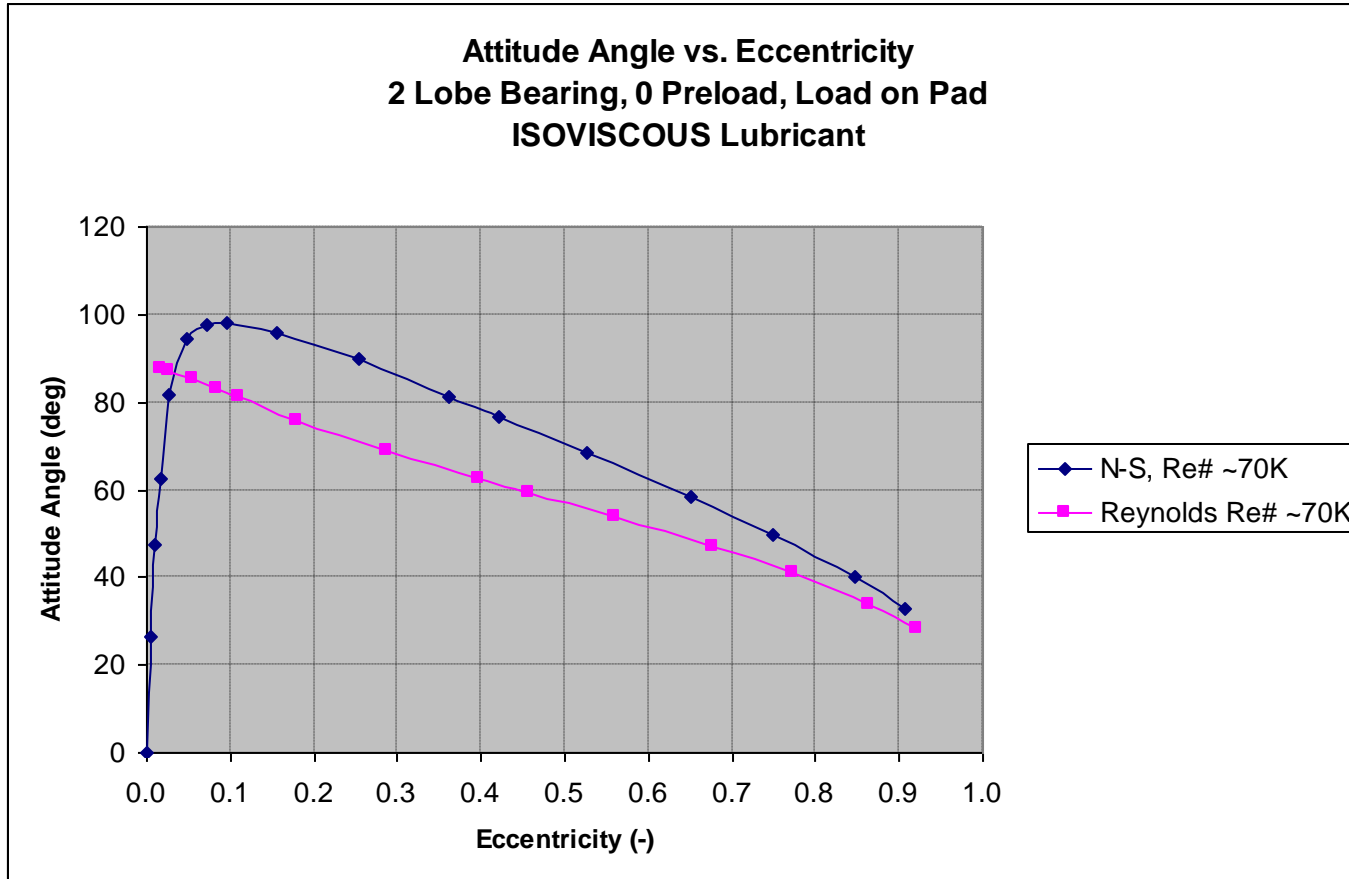
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# *Sample Calculations: Set 4*

## ➤ Journal Bearing Analysis

- 2 Lobe Fixed Geometry Bearing
  - » All Conditions Identical to Set 1 Calculations Except Rotor Speed and Viscosity
  - » Rotor Speed = 60000 rpm
- **Maximum Re# on Loaded Bearing Surface: ~70000**

# Fully Turbulent Flow Results



# *Fully Turbulent Flow Results*

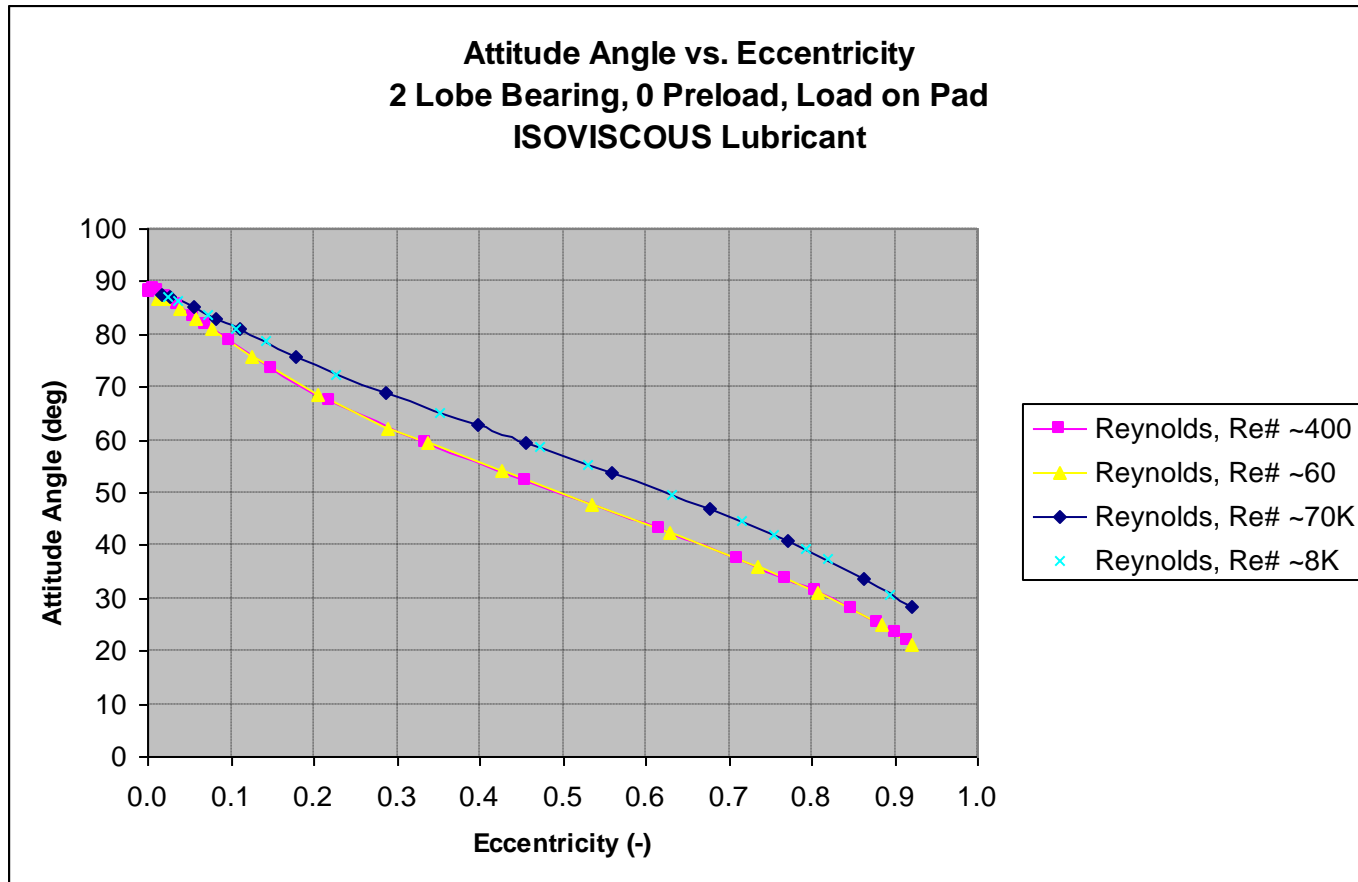
- **Journal Bearing Analysis: Max. Re# ~70000**
  - **Discussion of Results:**
    - » **Note: All Data Points Shown are For Identical Applied Loads**
    - » **Reynolds Equation Inaccurate At All Eccentricities**
      - **Results Only In the Ball Park for The Two Highest Eccentricity Cases ( $e > 80\%$ )**
    - » **Inertia Effects Substantial At All Eccentricities**

# *Reynolds Equation Summary*

- All Reynolds Equation Analysis Results (Fixed Geometry) are Plotted On the Following Page
  - Review of the Plot Shows:
    - » Reynolds Equation Offers a Binary Solution
      - ▣ Flow is Laminar (lower curve) or Turbulent (higher curve)
        - Locus of Centers, Regardless of Geometry or Operating Conditions, Will Fall on One of the Two Curves
        - Location on Curve Based Upon Sommerfeld Number (viscosity, diameter, length, load, clearance, and speed)
    - » Reynolds Equation Implicitly Assumes Away the Non-Linear Relationship Between Reynolds Numbers and Rotational Speed (i.e. ROTOR SPEED AND FLOW CONDITIONS DO NOT MOVE THE CURVES)



# Reynolds Equation Summary



# *Navier-Stokes Summary*

➤ All Navier-Stokes Equations Analysis Results (Fixed Geometry) are Plotted On the Following Page

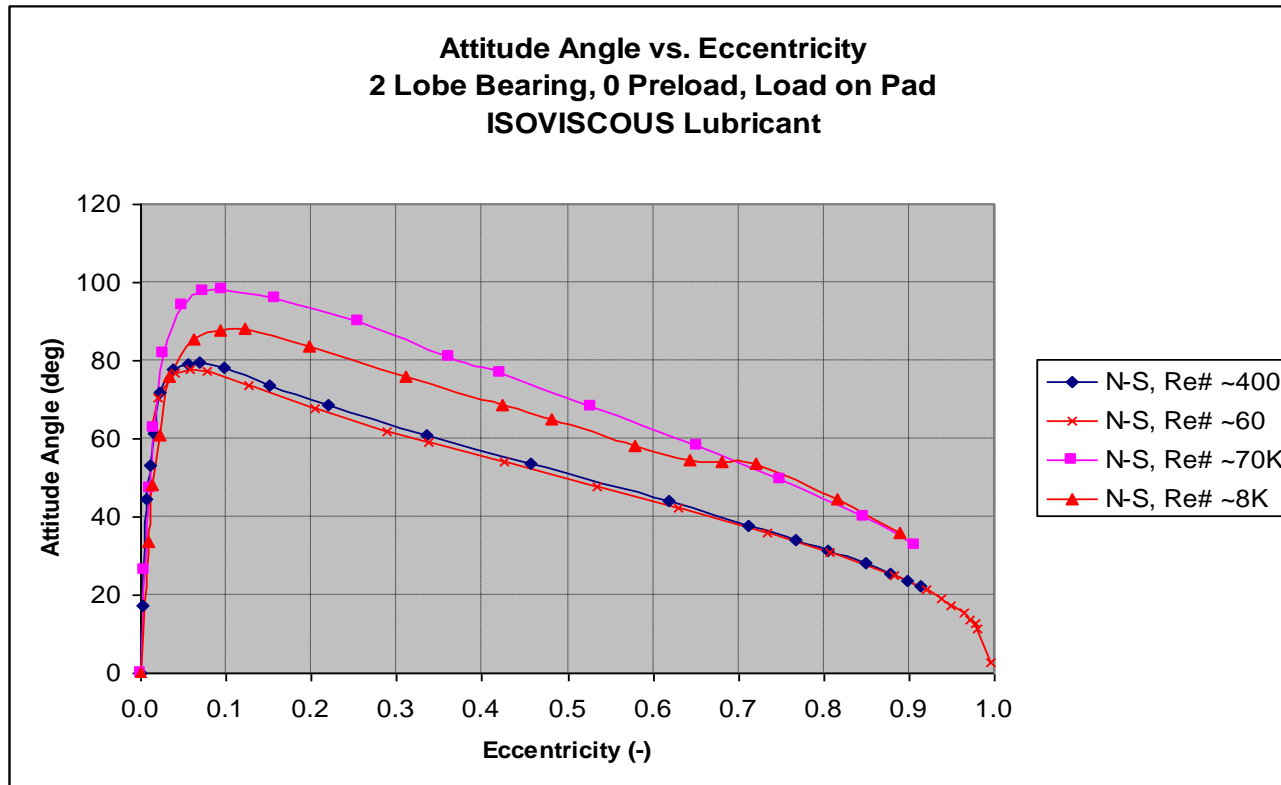
- Review of the Plot Shows:

- » **Navier-Stokes Equations are NOT a Binary Solution**

- Inertia Related Non-Linearities Prevalent Even in Laminar Flow
- Capable of Capturing Laminar to Turbulent Transitional Effects
  - Note Such Effects Persist Up to  $Re \# \sim 10000$
- Locus of Centers Curve Shape Determined Uniquely for Set of Geometry/Operating Conditions Analyzed
  - Curve May Assume Any Path Between the Fully Laminar and Fully Turbulent Flow Bounds

- » **Navier-Stokes Based Solution Implicitly Embodies a Non-Linear Relationship Between Reynolds Number and Rotor Speed (i.e. ROTOR SPEED AND FLOW CONDITIONS MOVE THE CURVES)**

# Navier-Stokes Summary



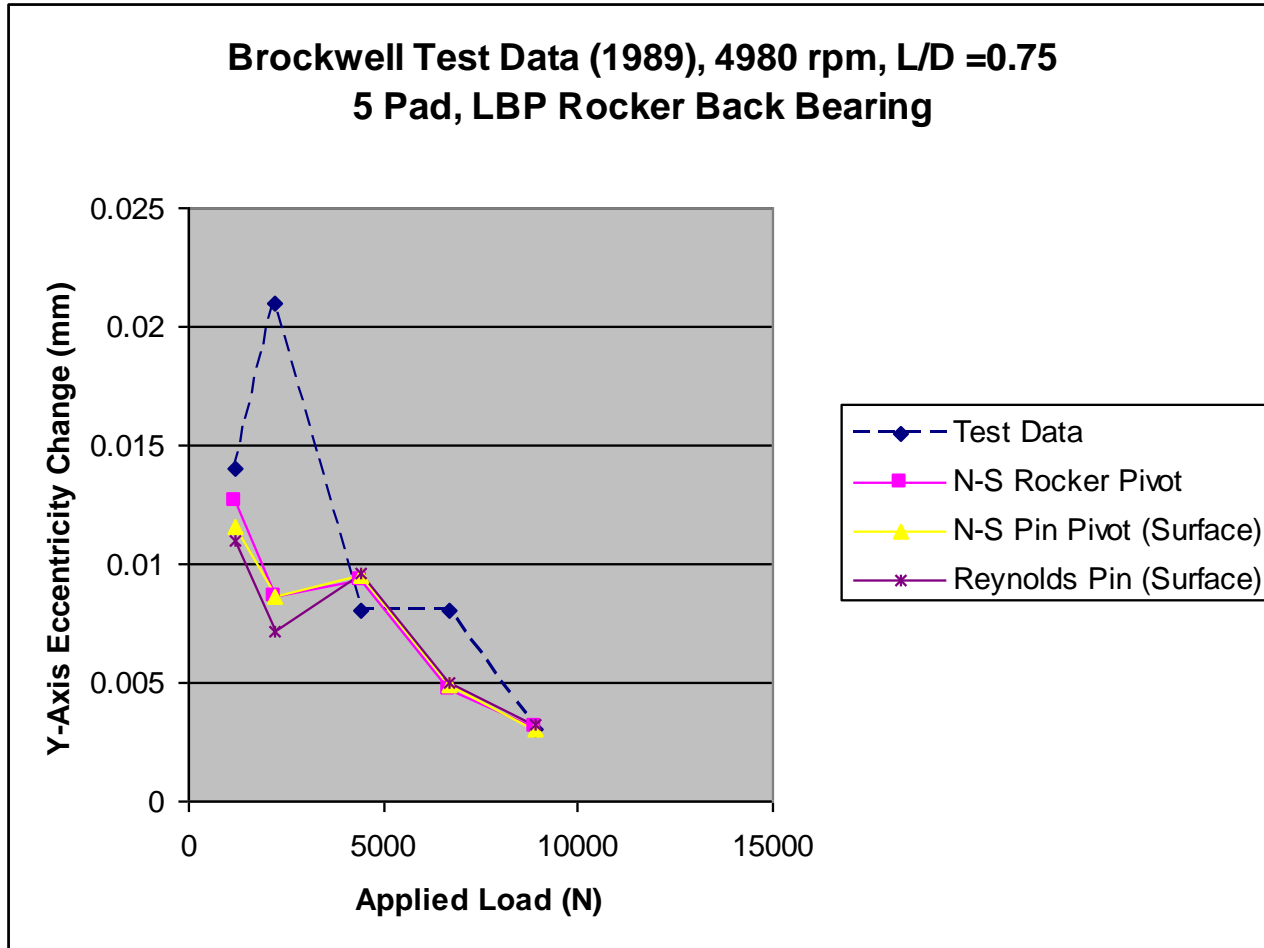
# Summary

- Reynolds Equation Based Bearing Analysis Only Agrees with N-S Based Analysis Under Certain Circumstances
  - Low Rotational Speeds ( $< \sim 10000$  rpm) **AND**
  - Low Reynolds Numbers ( $< \sim 60$ ) **AND**
  - Operating Conditions that Yield Eccentricities  $> 50\%$
- Reynolds Equation Based Bearing Analysis **MAY DIFFER RADICALLY** from N-S Based Solutions Under All Other Flow and Operating Conditions

# *Tilt Pad Bearing Analysis*

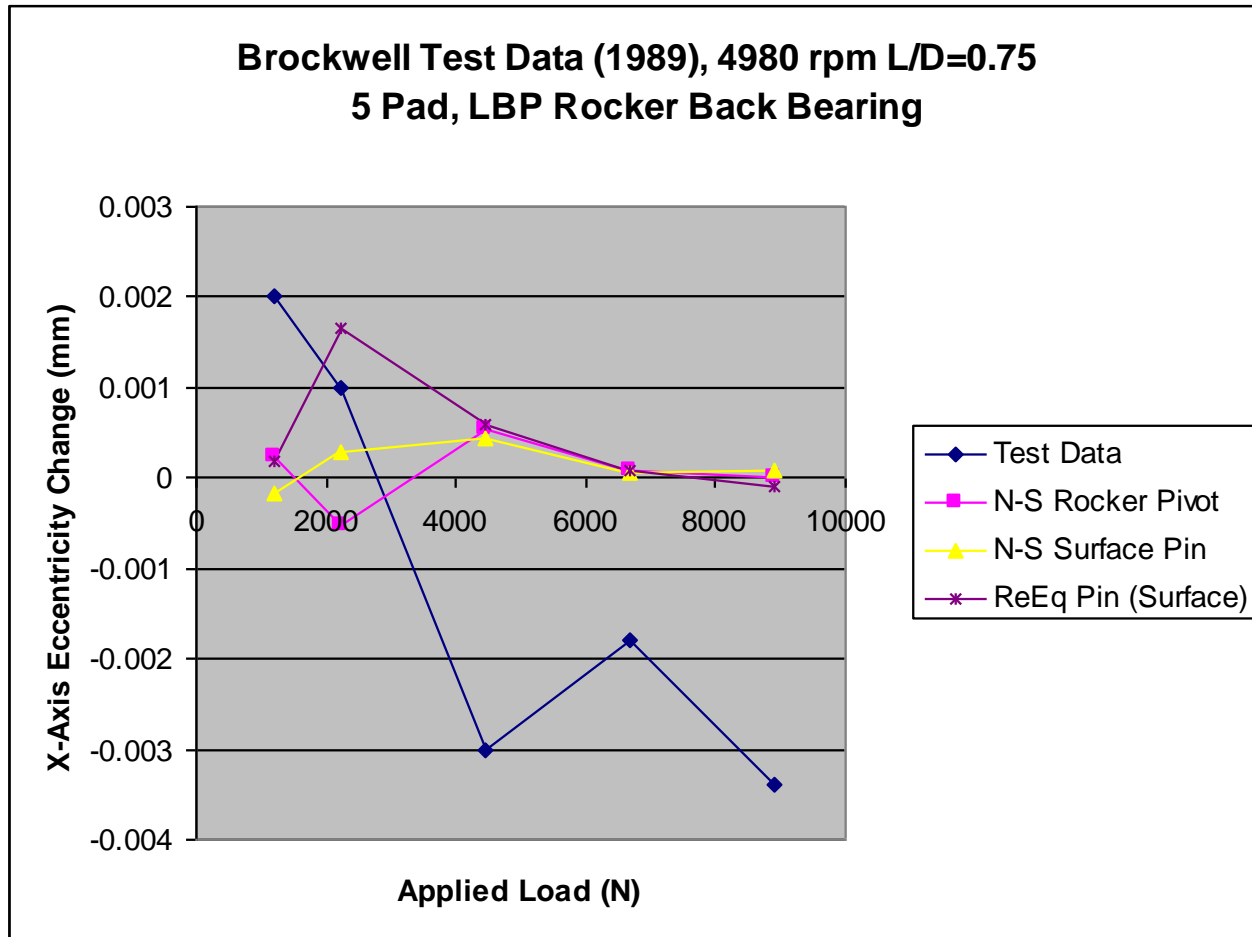
- Utilizes the Same N-S Stokes Film Solver as Fixed Geometry Bearings
  - Additional Iteration Loop Employed to Solve Pad Positions
  
- Pivot Models
  - Most Codes Assume Pads Rotate About a Point on the Load Bearing Surface
  - RSR has Implemented Advanced Pivot Models to More Accurately Represent the Motion of the Pad
    - » Pin Pivot
    - » Rocker Back
    - » Ball/Socket
  
- Sample Analysis Conducted to Match Test Data
  - 5 Pad, Rocker Back Bearing with Load Between Pads

# Tilting Pad Test Data Comparison



Reference: Measurements of the Steady State Operating Characteristics of the Five Shoe Tilting Pad Journal Bearing, K.R. Brockwell and D. Kleinbub, Tribology Transactions, 1989, pg 267-275

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# *Tilting Pad Test Data Comparison*

## ➤ Notes on Test Data

- Rotor Position Measurement was Sub Optimal
  - » 2 Sets of 2 Proximity Probes at Each End of Bearing
  - » Reported Results are the Average of the Two Readings
- Tests Utilizing 2 Sets of 4 Proximity Probes with Results Reported Independently Would Yield Better Data

## ➤ Comparison With Test Data

- Maximum Re# on Loaded Pads Varies Between 18 and 45
- Both N-S and ReEq Models Produce Reasonable Results
- N-S Predictions are Superior at Low Eccentricities (<50%)
- N-S with Advanced Pivot Model Provides Superior Predictions at Low Eccentricities (<35%)